## Superinfection between influenza and RSV alternating patterns in San Luis Potosí State, México. SUPPLEMENTARY MATERIAL

J.X. Velasco-Hernández M. Núñez-López A. Comas-García D. E. Noyola M. Capistrán

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We calculated  $R_0$  for both respiratory diseases using linear regression as described in the main text.

For Influenza and RSV we consider two outbreaks using the SIR model. In the following tables we list the estimated values for  $R_0$  for both diseases and for ARIs.

Table A: Estimated values of  $R_0$  for first outbreak of influenza for a SIR model

Year	$R_0$	β	$p ext{-}value$
2003	4.24	1.06	0.05
2004			
2005	_		
2006	3.67	0.92	0.74
2007	2.46	0.62	0.66
2008	2.21	0.55	0.05
2009	7	1.75	0.004

Table B: Estimated values of  $R_0$  for second outbreak of influenza for a SIR model

Year	$R_0$	β	$p ext{-}value$
2003	2.67	0.67	0.03
2004			
2005	2.97	0.74	0.008
2006		_	_
2007			
2008	_	_	_
2009	6.09	1.52	0.049

Table C: Estimated values of  $R_0$  for first outbreak of RSV.

Year	$R_0$	β	p-value
2003			
2004	2.28	0.46	0.03
2005	_	_	_
2006			
2007	_	_	_
2008	_	_	
2009	4.75	2.38	0.33

Table D: Estimated values of  $R_0$  for second outbreak of RSV

Year	$R_0$	β	p-value
2003	2.26	0.47	0.04
2004	8.9	1.78	0.005
2005	4.07	0.82	0.002
2006	2.45	0.49	0.02
2007	5.78	1.16	0.0003
2008	6.32	1.26	0.0008
2009			

Table E: Estimation of  $R_0$  for ARIs data from SIR model using influenza parameters

Year	$R_0$	β	p-value
2000	1.0035	0.2508	0.001
2001	1.0030	0.2507	0.003
2002	1.0034	0.2508	0.017
2003	1.0040	0.2510	0.005
2004	1.0067	0.2516	0.0005
2005	1.0078	0.2519	4.4e-5
2006	1.0064	0.2516	7.0e-10
2007	1.0023	0.2505	0.003
2008	1.0039	0.2509	2.0e-6
2009	1.0012	0.2503	0.0009
2010	1.0040	0.2510	1.4e-5

In figure 1 of the manuscript we show ARIs data from 2000-2010, so we present the replacement number  $R_e$  defined as the expected number of secondary infections that one infected person would produce through the entire duration of the infectious period (where the population need not be fully susceptible) for the total ARIs data; this is because all population is not susceptible at the beginning of each year [44].

Assuming that virus 1 is influenza and virus 2 is RSV, the replacement number of model (1) for each virus is given by

$$R_{e1} = \frac{\beta_1 \gamma_1}{(\mu + \eta_1)(\mu + \gamma_1)} (S + R_2), \qquad R_{e2} = \frac{\beta_2 \gamma_2}{(\mu + \eta_2)(\mu + \gamma_2)} (S + E_1 + I_1 + R_1)$$

where  $R_{e1}$  and  $R_{e2}$  are the replacement numbers for influenza and RSV respectively and with parameters  $\sigma = 0.7$ ,  $b_1 = 0.9162$  and  $b_2 = 0.4566$  we obtain  $R_{e1} = 3.62$  and  $R_{e2} = 0.07$ . Given the size of the basic reproduction and replacement numbers for RSV case so if  $R_{e2} < 1$  for  $R_{02} > 1$  either through an increase in the infectious population or the recovered population; in this case increases the infectious population of RSV and according to the model this makes it possible to infer the coexistence of both viruses where RSV superinfects influenza allowing it to survive.